Let 
$$A=\begin{bmatrix}2&3\\-1&1\end{bmatrix}$$
 and  $B=\begin{bmatrix}1&9\\-3&k\end{bmatrix}$ 

- a. What value(s) of k, if any, will make AB=BA? (Note a negative sign is pre-printed)
- b. For what value(s) of k are the columns of the following matrix linearly dependent?

$$\begin{bmatrix} 1 & -5 & 3 \\ 3 & -8 & -5 \\ -1 & 2 & k \end{bmatrix}$$

- c. Find the value(s) of k for which the matrix  $\begin{bmatrix} k^2 & 2k \\ 8 & k \end{bmatrix}$  is singular (i.e. not invertible).
- a. State your answer as a positive integer

-

b. State your answer as a positive integer.

c. State your answer as a positive integer.

± and □

a.

Let

$$A = \begin{bmatrix} 1 & -1 & 2 \\ -1 & 2 & 1 \\ 1 & -1 & 1 \end{bmatrix} \text{ and } \bar{b} = \begin{bmatrix} 5 \\ 6 \\ 2 \end{bmatrix}$$

- a. Find the inverse of A using elementary row operations and the identity matrix.
- b. Use the inverse of A to solve  $A\bar{x} = \bar{b}$
- a. State your answer as positive integers.

$$A^{-1} = \left[ \begin{array}{ccc} - & & & \\ - & & & \\ - & & & \\ 1 & & & - \end{array} \right]$$

Check Answer

b. State your answer as positive integers.

$$\overline{x} = \begin{bmatrix} 1 \\ \Box \\ \Box \end{bmatrix}$$

Consider the following linear system

$$\begin{array}{c} x_1+2x_2+x_3=1\\ -2x_1+x_2+x_3=-5\\ 2x_1-x_2-2x_3=a \end{array}$$

For which values of a is the system consistent?

Choose the correct answer below.

A For all real values of a

B For all real values of a except 5

C Only a = 5

igcup There are no values of a that make the system consistent

Only a=0 and 5

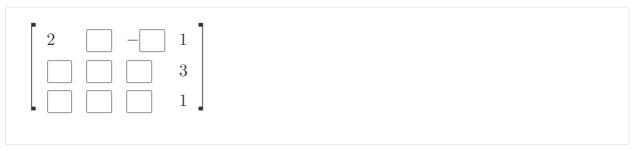
F Only a = 5 and -5

 $oldsymbol{\mathsf{G}}$  Only a=0 and 1

Let A be the matrix  $A = \begin{bmatrix} 4 & 8 & -2 \\ -6 & 2 & 10 \\ -2 & 6 & 6 \end{bmatrix}$ , and let  $\vec{b}$  be the vector  $\vec{b} = \begin{bmatrix} 2 \\ 18 \\ 15 \end{bmatrix}$ 

- a. Determine whether  $\vec{b}$  is in the span of the columns of A by finding echelon form of the augmented matrix.
- b. Let  $\vec{v}_1, \vec{v}_2$  and  $\vec{v}_3$  denote the columns of the matrix A. Is the set of vectors  $\{\vec{v}_1, \vec{v}_2, \vec{v}_3\}$  linearly independent or linearly dependent? If it is linearly dependent, find a linear dependency relation.
- a. State your answer as integers and then select the correct statement below.

## Echelon Form:



**Check Answer** 

- A The system is inconsistent which means that **b** is not in the span of the columns of *A*.
- B The system is consistent which means that **b** is not in the span of the columns of *A*.
- C The system is inconsistent which means that **b** is in the span of the columns of *A*.
- The system is consistent which means that **b** is in the span of the columns of *A*.

Check Answer

b. Select the correct item from the drop-down menu and then you may have to state the below dependence relation using positive integers as inputs.

The columns of A are linearly

$v_1 - v_2 + v_3 = 0$	
	Check Answer

a. Let three matrices be given by:

$$A = \begin{bmatrix} 1 & 1 & 0 \\ 0 & 1 & 1 \\ 0 & 0 & 1 \end{bmatrix}, \quad B = \begin{bmatrix} 2 & 0 & 0 \\ 1 & 1 & 2 \\ 2 & 0 & 1 \end{bmatrix}, \quad C = \begin{bmatrix} 1 & 1 & 0 \\ 0 & 1 & 0 \\ 0 & 1 & 2 \end{bmatrix}$$

Find the determinant of matrix X in the following matrix equation XA = XB + C. State your answer as an integer between 0 and 99.

In Python, you can find the determinant of a Sympy Matrix A using A.Det() or Det(A)

$$\det X = \square$$

Let A be the following matrix:

$$\begin{bmatrix} 1 & 3 \\ -2 & -8 \end{bmatrix}$$

a. Find numbers p and q, such that  $A^2=pA+qI$ , where I is the  $2\times 2$  identity matrix. Notice a negative sign is preprinted

$$p = -$$

$$q =$$

b. Let B=A-tI, where t is a scalar. For which values of t is B not invertible? State your answer as a positive integer.

$$t = \pm \frac{\sqrt{\square}}{2} - \frac{7}{2}$$

## Item 7

This is challenge exercise. You do not need to do it in order to get 100%.

Given the three matrices

$$A = \begin{bmatrix} -1 & 2 \\ 1 & 1 \end{bmatrix}, \quad B = \begin{bmatrix} 1 & 2 \\ 0 & 1 \end{bmatrix}, \quad C = \begin{bmatrix} 2 & 2 \\ 3 & 1 \end{bmatrix}$$

solve the following system of matrix equations (i.e. find matrices X and Y)

$$\begin{cases} AX + CY = BAC \\ CX - BY = CAB \end{cases}$$

and state the determinants of X and Y. State your answers as integers between 0 and 99.

$$\det X = -\frac{36}{\Box}, \quad \det Y = \boxed{\phantom{A}}$$